

reis de Référence Temps-Espace

The astronomical units

Nicole Capitaine and Bernard Guinot

Observatoire de Paris / SYRTE, 61 Avenue de l'Observatoire 75014 Paris

Introduction

The IAU-1976 System of astronomical constants includes 3 astronomical units:

- The astronomical unit of time, i.e. the day (D),
 is related to the SI second by a defining number (D=86400 s),
 - its role is to provide a unit of time of "convenient" size for astronomy, as is the Julian century of 36 525 days,
 - the "day" appears in the SI Brochure (Table 6), along with the minute and the hour, as one of the "Non-SI units accepted for use with the International System of Units".

The astronomical unit of length, ua, and the mass of the Sun, Ms.

- · are specific astronomical units for expressing distances and masses in the solar
- the best estimated values in SI of these astronomical units have been regularly improved in the successive lists of numerical standards (c.f. Standish 1995, 2004),
- although these two astronomical units are still acknowledged as being appropriate for expressing distances and masses in the solar system, the current definition and use of the ua lead to some ambiguities and difficulties

1st system of fundamental astronomical constants (Conférence internationale des étoiles fondamentales, Paris, 1896)

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1º La constante de la précession
                                             = 50",2564;
2º La constante de la nutation
                                    .. N_0 = 9'', 21;
... i = 23^{\circ}27'8'', 26;
3º L'obliquité de l'écliptique
4º La constante de l'aberration
50 La parallaxe solaire
6º L'aplatissement de l'ellipsoïde
    terrestre
                                      z = 1/297;
7º Le rayon équatorial terrestre
                                   .. a. = 6 378 388 m
8º La constante de la gravitation
                        k = 0.01720209895
    universelle
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The IAU 1976 System of astronomical constants

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    Gaussian gravitation
    Speed of light

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c = 299 \ 792 \ 458 \ m \ s^{-1}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               \begin{split} & \tau_{\rm A} = (90.004~72.5~;\\ & - (900.004~72.5~;\\ & - (900.004~23.80~;)\\ & - (9.75~10.7)\\ & - (9.07~10.70~;\\ & - (9.07~10.70~;\\ & - (9.01~00.2~3.5)\\ & - (9.01~00.2~3.5)\\ & - (9.01~00.2~3.70~;\\ & - (9.01~00.2~3.70~;\\ & - (9.01~00.2~3.70~;\\ & - (9.01~00.2~3.70~;\\ & - (9.01~00.2~3.70~;\\ & - (9.01~00.2~3.70~;\\ & - (9.01~00.2~3.70~;\\ & - (9.01~00.2~3.70~;\\ & - (9.01~00.2~3.70~;\\ & - (9.01~00.2~3.70~;\\ & - (9.01~00.2~3.70~;\\ & - (9.01~00.2~3.70~;\\ & - (9.01~00.2~3.70~;\\ & - (9.01~00.2~3.70~;\\ & - (9.01~00.2~3.70~;\\ & - (9.01~00.2~3.70~;\\ & - (9.01~00.2~3.70~;\\ & - (9.01~00.2~3.70~;\\ & - (9.01~00.2~3.70~;\\ & - (9.01~00.2~3.70~;\\ & - (9.01~00.2~3.70~;\\ & - (9.01~00.2~3.70~;\\ & - (9.01~00.2~3.70~;\\ & - (9.01~00.2~3.70~;\\ & - (9.01~00.2~3.70~;\\ & - (9.01~00.2~3.70~;\\ & - (9.01~00.2~3.70~;\\ & - (9.01~00.2~3.70~;\\ & - (9.01~00.2~3.70~;\\ & - (9.01~00.2~3.70~;\\ & - (9.01~00.2~3.70~;\\ & - (9.01~00.2~3.70~;\\ & - (9.01~00.2~3.70~;\\ & - (9.01~00.2~3.70~;\\ & - (9.01~00.2~3.70~;\\ & - (9.01~00.2~3.70~;\\ & - (9.01~00.2~3.70~;\\ & - (9.01~00.2~3.70~;\\ & - (9.01~00.2~3.70~;\\ & - (9.01~00.2~3.70~;\\ & - (9.01~00.2~3.70~;\\ & - (9.01~00.2~3.70~;\\ & - (9.01~00.2~3.70~;\\ & - (9.01~00.2~3.70~;\\ & - (9.01~00.2~3.70~;\\ & - (9.01~00.2~3.70~;\\ & - (9.01~00.2~3.70~;\\ & - (9.01~00.2~3.70~;\\ & - (9.01~00.2~3.70~;\\ & - (9.01~00.2~3.70~;\\ & - (9.01~00.2~3.70~;\\ & - (9.01~00.2~3.70~;\\ & - (9.01~00.2~3.70~;\\ & - (9.01~00.2~3.70~;\\ & - (9.01~00.2~3.70~;\\ & - (9.01~00.2~3.70~;\\ & - (9.01~00.2~3.70~;\\ & - (9.01~00.2~3.70~;\\ & - (9.01~00.2~3.70~;\\ & - (9.01~00.2~3.70~;\\ & - (9.01~00.2~3.70~;\\ & - (9.01~00.2~3.70~;\\ & - (9.01~00.2~3.70~;\\ & - (9.01~00.2~3.70~;\\ & - (9.01~00.2~3.70~;\\ & - (9.01~00.2~3.70~;\\ & - (9.01~00.2~3.70~;\\ & - (9.01~00.2~3.70~;\\ & - (9.01~00.2~3.70~;\\ & - (9.01~00.2~3.70~;\\ & - (9.01~00.2~3.70~;\\ & - (9.01~00.2~3.70~;\\ & - (9.01~00.2~3.70~;\\ & - (9.01~00.2~3.70~;\\ & - (9.01~00.2~3.70~;\\ & - (9.01~00.2~3.70~;\\ & - (9.01~00.2~3.70~;\\ & - (9.01~00.2~3.70~;\\ & - (9.01~00.2~3.70~;\\ & - (9.01~00.2~3.70~;\\ & - (9.01~00.2~3.70~;\\ & - (9.01~

    Constant of gravitation
    Ratio of mass of Moon to that of Earth

    General precession in longitude, per Julian century, at standard epoch 2000

Obligaty of the ecliptic, at standard epoch 2000

                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       e = 23° 26′ 21′448
| Definition | Constants | Co
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Aim of this presentation: to discuss the status of the astronomical unit of length and mass within the modern context

The current definition of the astronomical unit of length (ua)

Definition of the ua in the IAU-1976 System of astronom ical constants

The astronomical unit of length is that length (A) for which the Gaussian gravitational constant (k) takes the value of 0.017 202 098 95 when the units of measurements are the astronomical unit of length, mass and time. The dimensions of k^2 are those of the constant of gravitation (G), i.e., $L^3M^+T^-^2$. The term "unit distance" is also for the length A.

Definition of the of the ua in the SI brochure (intended to non-astronomers

The astronomical unit is approximately equal to the mean Earth-Sun distance. It is the radius of an unperturbed circular Newtonian orbit about the Sun of a particle having infinitesimal mass, moving with a mean motion of 0.017 202 098 95 radians per day (known as the Gaussian constant).

The current definition of the ua is complicated and obscure for non-experts, and very difficult to teach to students

The IAU-1976 gravitational constant constant related to the mass of the Sun

- The IAU 1976 heliocentric gravitational constant, GM_{Sun} , is a "derived constant", which can be expressed as: GM_{Sun} = $(ua)^3\,k^2\,D^{-2}$,
 - → the SI value of GM_{sun} is derived from the SI values for the ua and the day.
- The estimation of the mass of the Sun in kg has to be derived from the SI values of (1) GM_{Sun} and (2) the gravitational constant G (current relative uncertainty~ 1x10-4).
- The mass of the Sun in kg is provided in the numerical standards in astronomy, but is not provided in the SI brochure

SI brochure, Table 7 (<u>Section 4.1</u>)					The IERS Conventions 2003					
Table 7. Non-SI units whose values in SI units must be obtained experimentally					Table	1.1 IERS Numerical Stan M VALUE 290792458ms ⁻¹	dards. UNCERTAINTY Defining	REF.	COMMENTS Speed of light	
Quantity	Name of unit	Symbol for unit	Value in SI units (4)		L_B L_C	$1.55051976772 \times 10^{-8}$ $1.48082686741 \times 10^{-8}$	2×10^{-17} 2×10^{-17}	[4] [4]	Average value of 1-d(TT)/d(TCB) Average value of 1-d(TCG)/d(TCl	
Units accepted for use with the SI					L _G	$6.969290134 \times 10^{-10}$ $6.673 \times 10^{-11} m^2 ka^{-1} s^{-1}$	Defining $1 \times 10^{-13} m^2 k a^{-1} s^{-2}$	[4] [2]	1-d(TT)/d(TCG) Constant of gravitation	
energy	electronvolt (9)	eV	1 eV = 1.602 176 53 (14) × 10 ⁻¹⁹ J		GM.			[2]		
mass	dalton, (c)	Da	1 Da = 1.660 538 86 (28) x 10 ⁻²⁷ kg		Tat	499.0047838061s	0.00000002s /	[3]	Astronomical unit in seconds	
	unified atomic mass unif	u .	1 u = 1 Da		CTA [†]	149597870691m	6m	[3]	Astronomical unit in meters	
	astronomical unit				ψ ₁ †	5038.47875"/c	0.00040"/c	[6]	IAU(1976) value of precession of	
length	(4)	US	1 us = 1.495 978 706 91 (6) x 10 ¹¹ m						the equator at J2000.0 corrected	
		Natural or	its (n.u.)						by -0.29965". See Chapter 5.	
speed	n.u. of speed (speed of light in vacuum)	00	299 792 458 m/s (exact)		69	84381.4059"	0.0003"	[5]	Obliquity of the ecliptic at J2000.0. See Chapter 5 for value used in IAU precession-nutation model.	
action	n.u. of action (reduced Planck constant)	л	1.054 571 68 (18) × 10 ⁻³⁴ J s		$J_{2\odot}$ μ	2×10^{-7} 0.0123000383	(adopted for DE405) 5×10^{-10}	[3]	Dynamical form-factor of the Sun Moon-Earth mass ratio	
mass	n.u. of mass (electron mass)	m _e	9.109 3826 (16) x 10 ⁻⁸¹ kg		GM	$0.3.986004418 \times 10^{14} m^3 s^{-2}$	$8 \times 10^{5} m^{3} s^{-1}$	[1]	Geocentric gravitational constant (EGM96 value)	
time	n.u. of time	$N(m_e c_0^2)$	1.288 088 6677 (86) x 10 ⁻²¹ s		ag:	6378136.6m	0.10m	[1]	Equatorial radius of the Earth	
		Atomic un	its (a.u.)		$1/f^{1}$		0.00001	[1]	Flattening factor of the Earth	
charge	a.u. of charge (elementary charge)		1.602 176 53 (14) × 10 ⁻¹⁹ C		J ₂₀ ; ω	1.0826359×10^{-2} $7.292115 \times 10^{-5} rads^{-1}$	1.0×10^{-10} variable	[1] [1]	Dynamical form-factor Nominal mean angular velocity of the Earth	
mass	e.u. of mass (electron mass)	m _e	9.109 3826 (16) x 10 ⁻³¹ kg		g _e ! Wo	$9.7803278ms^{-2}$ $62636856.0m^2s^{-2}$	$1 \times 10^{-6} ms^{-2}$ $0.5 m^2 s^{-2}$	[1]	Mean equatorial gravity Potential of the geoid	
action	a.u. of action (reduced Planck constant)	ň	1.054 571 60 (10) × 10 ⁻³⁴ J s		Ro11	6363672.6m	0.1m	[1] [1]	Geopotential scale factor	
length	a.u. of length, bohr (Bohr radius)	00	0.529 177 2108 (18) × 10 ⁻¹⁰ m	 The values for τ_A, στ_A, and ψ₁ are given in "TDB" units (see dimension above). The values for σ_B, γ_I/f, φ_B and g_B are "zero tide" values (see the discussion in section 1.1 above). Values according to other correctations may be found from reference (1). R_D = OM_D/W_O 						
energy	a.u. of energy, hartree (Hartree energy)	£h	4.359 744 17 (75) × 10 ⁻¹⁶ J							
time au. of time MPS, 24,80 84,26 505 (16) x 10 ⁻¹² 5 (3) The statements unit is approximately equal to the mean Earl-Son distator, 11, 11 to leave the statement of the statem					 Groton, E., 1999, Report of the IAC. Special Commission SCS, Paulamental Constant XXII IAC General Assembly Mohr, P. J. and Tayles, B. N., 1999, J. Phys. Chem. Ref. Data, 28, 6, p. 1713. Standrah, B. M., 1999, J. P. 100M 312-P. Ida U. XXV General Assembly. See Appendix Ida U. XXV General Assembly. See Appendix Most Description of Astronomy, in the Commission of Commission of Astronomy, in the Commission of Astronomy, in matter acress for Energy In Commission of Commission of Commission of Commission of the Commission of Commission of					

The role of the of the astronomical unit of length (ua): simplified outline

For historical reasons, the ua is defined by the value of the Gaussian gravitational constant ${\bf k}$ (with $k^2=G$), called a "defining constant", and the 3d Kepler's law ($n^2a^3=GM_S$ for a planet of negligible mass).

Official situation (IAU-1976)

- GM_{Sun} is fixed by convention,
- for a fictitious planet with an infinitesimal mass, n =n₀ by convention,
- for any planet, n is measured in SI -> a in ua.

The precision of the time measurements is reported into the relative distances

There is no special link to the SI.

Current practical situation

- for any planet, n is measured in SI
- ua is measured in SI

GM_{Sun} is estimated

- the ua appears in the current version of the SI Brochure (Table 7) as being one of the "Non-SI units whose values in SI units must be obtained experimentally

Changes in the status of the ua and GM_{S} since the adoption of the IAU-1976 System

The context of the recent IAU Resolutions on reference systems

The celestial reference systems have been defined in a GR framework (IAU Resolutions 1991: GR framework; IAU 2000: GCRS, BCRS, re-definition of TT, IAU 2006: re-definition of TDB).

The context of the modern observations in the solar system

High accuracy observations are mainly based on range and Doppler measurements, especially for terrestrial bodies (Moon, Mercury, Venus, Mars, \dots).

The context of the recent ephemeric

According to recent publications

- the GM_i of the planets are actually estimated in SI (TDB-compatible) in the JPL ephemerides (Folkner et al. 2008),
- GM_{sus} will be estimated in future version of the INPOP ephemerides (Fienga et al. 2008).

The status of the ua and GM_S should be reformed to be more in agreement with the modern context.

Discussion: interpretation based on recent ephemerides publications

For the terrestrial bodies, for which there are very precise range and Doppler measurements, GM_{Sun} can be estimated with a very high precision,

- this defines the scale for the distances in the solar system with high precision

For the planets, for which observations are mainly angular measurements (Jupiter, Saturn, etc.),

- the relative distances of the planets are determined as with old observations.
- the scale in SI of the global solution is provided by the GM_{Sun} value determined by the terrestrial bodies (heigh weight) \rightarrow distances in SI.

If very precise angular measurements of the planets expressed in an unit linked to GM_{sun} are available.

- the relative distances can be determined with very high precision,
- → the (absolute) distances in SI may be different, but are with the same ratio

Suggested reform in the status of the astronomical units

Several options can be considered in the GR context (Guinot 1995, Capitaine & Guinot 1995, Klioner 2007).

There are two possibilities in the Newtonian context (compatible with GR):

- $\mbox{GM}_{\mbox{\scriptsize Sun}}$ fixed and ua estimated in SI,
- GM_{Sun} estimated in SI and ua fixed in SI.

Estimating $\mathrm{GM}_{\mathrm{Sun}}$ is the option that has the most physical meaning since it does not suppose that the mass of the Sun is constant.

Conclusion

- A re-definition of the ua is necessary in the modern context in order to make the system of astronomical constants best compliant with modern dynamical astronomy.
- The ua should be re-defined as an astronomical unit of length defined trough a fixed relation to the SI meter by a defining number.
- From the point of view of the principles, the important point is the change of status for the astronomical unit of length (and not the value of its defining number).
- · This would mean:
- dropping the k constant (and implicitly GM_{Sun}=constant), and abandoning the experimental determination of the ua in SI unit.
- determining experimentally GMs, which would not be considered any more as being a "constant", - limiting the role of the ua to that of a unit of length of "convenient" size for solar system
- · Such a change of status of the ua would:
- be a great simplification for the users of the astronomical constants (i.e. the ua would have a fixed numerical value in meters)
 - let appear directly the possible variation of the mass of the Sun, and/or of G.

References

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